Spring 2010 Released Test

# END OF COURSE GEOMETRY 

## Form M0110, CORE 1

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## Geometry Formula Sheet

## Geometric Formulas


$A=\frac{1}{2} h\left(b_{1}+b_{2}\right)$
$V=B h$
$L . A .=h p$
S.A. $=$ L.A. $+2 B$

$A=\pi r^{2}$
$C=2 \pi r$
$V=\pi r^{2} h$
L.A. $=2 \pi r h$
S.A. $=2 \pi r(h+r)$

$V=\frac{1}{3} \pi r^{2} h$
L.A. $=\pi r l$
$S . A .=2 l w+2 l h+2 w h$

$V=\frac{1}{3} B h$ $L . A .=\frac{1}{2} l p$
$S . A .=L . A .+B$


$$
V=\frac{4}{3} \pi r^{3}
$$

$$
S . A .=4 \pi r^{2}
$$



$$
c^{2}=a^{2}+b^{2}
$$

Geometric Symbols

| Example | Meaning | Example | Meaning |
| :---: | :---: | :---: | :---: |
| $\angle A$ | angle $A$ | $\overrightarrow{A B}$ | vector $A B$ |
| $\mathrm{m} \angle A$ | measure of angle $A$ | $\downarrow$ | right angle |
| $\stackrel{\text { AB }}{ }$ | line segment $A B$ | $\overleftrightarrow{A B} \\| \overleftrightarrow{C D}$ | Line $A B$ is parallel to line $C D$. |
| $A B$ | measure of line segment $A B$ | $\overleftrightarrow{A B} \perp \overleftrightarrow{C D}$ | Line $A B$ is perpendicular to line $C D$. |
| $\overleftrightarrow{A B}$ | line $A B$ | $\angle A \cong \angle B$ | Angle $A$ is congruent to angle $B$. |
| $\triangle A B C$ | triangle $A B C$ | $\triangle A \sim \triangle B$ | Triangle $A$ is similar to triangle $B$. |
| $\square A B C D$ | rectangle $A B C D$ |  | Similarly marked segments are congruent. |
| $\checkmark A B C D$ | parallelogram $A B C D$ | $A \square$ | Similarly marked angles are congruent. |

Abbreviations

| Volume | $V$ |
| :--- | :--- |
| Lateral Area | L.A. |
| Total Surface <br> Area | S.A. |
| Area of Base | $B$ |

## Pi

$\pi \approx 3.14$
$\pi \approx \frac{22}{7}$

## Directions

Read each question and choose the best answer.

## SAMPLE



If $\triangle A B C$ is similar to $\triangle A D E$, then $A B: A D=$ ?: $A E$. Which replaces the "?" to make the statement true?

A $A C$
B $A E$
C $D E$
D $B C$

## 1 A bisector of $\overline{A B}$ contains which line segment?

$$
\bullet C \quad \bullet E
$$

$$
\bullet D
$$


$\bullet F \quad \bullet G$
A $\overline{C G}$
B $\overline{D F}$
C $\overline{D G}$
D $\overline{E F}$

2 Lines $m$ and $r$ are cut by a transversal.


What value of $x$ will show that line $m$ is parallel to line $r$ ?
F 20
G 24
H 25
J 33


If lines $a$ and $b$ are parallel, what is the value of $\boldsymbol{x}$ ?
A 120
B 115
C 65
D 60

4 Which point lies on the bisector of angle $P Q R$ ?

$\begin{array}{ll}\mathbf{F} & W \\ \mathbf{G} & X \\ \mathbf{H} & Y \\ \mathbf{J} & Z\end{array}$

5 For what measure of $\angle D$ is $\overline{A B} \| \overline{D C}$ in this figure?


A $26^{\circ}$
B $59^{\circ}$
C $69^{\circ}$
D $95^{\circ}$


Which line segment is congruent to $\overline{B C}$ ?
F $\overline{P Q}$
G $\overline{P R}$
H $\overline{P S}$
J $\overline{P T}$

7 In the figure shown, line $q$ is a transversal of parallel lines $l, m, n$, and $p$.


What are the values of $x$ and $y$ ?
A $x=30, y=30$
B $x=30, y=150$
C $x=150, y=30$
D $x=150, y=150$

8 In the figure shown, parallel lines $\boldsymbol{j}$ and $\boldsymbol{k}$ are cut by transversal $\boldsymbol{m}$.


What is $m \angle 1$ ?
F $32^{\circ}$
G $58^{\circ}$
H $122^{\circ}$
J $148^{\circ}$

9 Lines $y$ and $z$ are cut by a transversal.


For what value of $x$ is $y \| z$ ?
A 13
B 77
C 103
D 154

10 In this figure, $m \angle 1=(15 x-5)^{\circ}$ and $m \angle 2=(10 x+35)^{\circ}$.


What is $m \angle 1$ ?
F $31^{\circ}$
G $65^{\circ}$
H $85^{\circ}$
J $115^{\circ}$

11 This figure represents line segments painted on a parking lot to create parking spaces.


Which equation can be used to show that these line segments are parallel?
A $\quad 118-w=x$
B $\quad 118-x=w$
C $\quad x+118=180$
D $w+118=180$

12 Given: $\triangle A B C \sim \triangle L M N$


What is the length of $\overline{A C}$ ?
F $\quad 11$
G $\quad 12$
H 22
J 24

13 Given the following measures of the sides of triangles, which is a right triangle?

A $41 \mathrm{~cm}, 40 \mathrm{~cm}, 9 \mathrm{~cm}$
B $45 \mathrm{ft}, 40 \mathrm{ft}, 35 \mathrm{ft}$
C 52 in., 50 in., 11 in.
D $45 \mathrm{yd}, 35 \mathrm{yd}, 25 \mathrm{yd}$


Which of the following statements must be true about this Venn diagram?
F All rectangles are rhombi.
G Some rhombi are rectangles.
H Quadrilaterals are not rhombi or rectangles.
J All quadrilaterals are rhombi and rectangles.

15 Given: In this figure, $\overline{A C}$ and $\overline{B D}$ bisect each other.


Based on the information given, which triangle congruence theorem could be used to prove $\triangle A E D \cong \triangle C E B$ ?

A Angle-Angle-Side (AAS)
B Angle-Side-Angle (ASA)
C Side-Angle-Side (SAS)
D Side-Side-Side (SSS)

16 Statement: If lines are skew, then they are not coplanar.
What is the contrapositive of the statement?
F If lines are not coplanar, then they are skew.
G If lines are not skew, then they are coplanar.
H If lines are coplanar, then they are not skew.
J If lines are skew, then they are coplanar.

17 Coordinates $A(2,5), B(6,4)$, and $C(6,0)$ are connected to form $\triangle A B C$.


If $\triangle C D A$ is congruent to $\triangle A B C$, what are the coordinates of $D$ ?
A $(1,1)$
B $(1,2)$
C $(2,2)$
D $(2,1)$

18 Let $p=A n$ equation is of the form $y=m x+b$.
Let $q=$ Its graph is a line.
Argument: If an equation is of the form $y=m x+b$, then its graph is a line. The graph is not a line.
Therefore, the equation is not of the form $y=m x+b$.
Which of the following is the symbolic representation of the given argument?

F $\quad \begin{aligned} & p \rightarrow q \\ & \sim q \\ & \therefore \sim p\end{aligned}$

G $\quad \begin{aligned} & p \rightarrow q \\ & q \\ & \therefore p\end{aligned}$

H $\quad \begin{aligned} & p \rightarrow q \\ & \sim p \\ & \therefore \sim q\end{aligned}$

J $\quad \begin{aligned} & p \rightarrow q \\ & p \\ & \therefore q\end{aligned}$
$19 \Delta T R G$ is a right triangle.


Which is closest to the length of $\overline{R T}$ ?
A 5
B 11
C $\quad 14$
D 28


Which list has the sides of $\triangle A B C$ ordered from longest to shortest?
F $\overline{B C}, \overline{A C}, \overline{A B}$
G $\overline{A B}, \overline{A C}, \overline{B C}$
H $\overline{A C}, \overline{A B}, \overline{B C}$
J $\overline{B C}, \overline{A B}, \overline{A C}$

21 Three survey markers are located on a map at points $H, I$, and $J$. A triangle is formed by connecting these markers by string so that $H I=150$ feet, $H J=245$ feet, and $I J=365$ feet .

Which statement is true about the measures of the angles of $\triangle H I J$ ?
A $m \angle H$ is the smallest
B $m \angle H$ is the largest
C $m \angle I$ is the smallest
D $m \angle I$ is the largest


In the figure, what is the value of $\boldsymbol{x}$ ?
F 6
G $6 \sqrt{2}$
H $6 \sqrt{3}$
J 12

23 Two sides of a triangle measure 14 inches and 8 inches. Which cannot be the length of the remaining side?

A 6 in.
B 8 in .
C 14 in .
D 21 in .


In the circle, what is the measure of $\angle A B C$ ?

$$
\begin{array}{ll}
\mathbf{F} & 30^{\circ} \\
\mathbf{G} & 60^{\circ} \\
\mathbf{H} & 120^{\circ} \\
\mathbf{J} & 140^{\circ}
\end{array}
$$

25 This figure shows a pattern of triangles and regular hexagons.


What is the value of $x$ ?
A 30
B 60
C 90
D 120

26 Which figure has all sides of equal measure but not necessarily all angles of equal measure?

F Square
G Rectangle
H Rhombus
J Trapezoid

27 What is $m \angle D A R$ in circle $A$ ?


A $\quad 17^{\circ}$
B $34^{\circ}$
C $56^{\circ}$
D $68^{\circ}$

28 Two chords intersect with the measures shown in the drawing.


What is the value of $x$ ?
F 8.0
G 9.5
H 10.0
J 14.5

29 In rectangle $A B C D$, the slope of $\overline{A B}$ is $\frac{1}{2}$. What is the slope of $\overline{C D}$ ?
A -2
B $\quad-\frac{1}{2}$
C $\frac{1}{2}$
D 2

30 In the figure shown, what is $m \angle W X Y$ ?


F $45^{\circ}$
G $107^{\circ}$
H $120^{\circ}$
J $135^{\circ}$
$31 D E F G$ is a rhombus with $m \angle E F G=28^{\circ}$.


What is $m \angle G D E$ ?
A 140
B $28^{\circ}$
C $30^{\circ}$
D $56^{\circ}$

32 This figure is a traffic sign in the shape of a regular octagon.


What is the value of $x$ ?
F 45
G 60
H 135
J 180

33 A rectangular rug is $\mathbf{2 4}$ feet long and $\mathbf{1 0}$ feet wide. A rhombus design is formed inside the rug by joining the midpoints of each side of the rectangle. What is the length of each side of the rhombus?

A 13 ft
B 26 ft
C 169 ft
D 240 ft

34 A man who is 6 feet tall casts a shadow that is $\mathbf{4}$ feet long. At the same time, a nearby flagpole casts a shadow that is $\mathbf{1 8}$ feet long. How tall is the flagpole?

F 10 ft
G 12 ft
H 22 ft
J 27 ft

35 A fish tank in the shape of a rectangular prism has these dimensions:

- length $=20$ inches
- width $=10$ inches
- height = $\mathbf{1 2}$ inches

What is the volume of water in the tank when it is $\frac{4}{5}$ full?
A $1,120 \mathrm{cu}$ in.
B $1,920 \mathrm{cu} \mathrm{in}$.
C $2,400 \mathrm{cu} \mathrm{in}$.
D $3,000 \mathrm{cu} \mathrm{in}$.

36 Which of these nets would form a cube when folded?
F

G

H

J


37 If a cube with side length 6 inches has its dimensions divided in half, what will be the volume of the new cube?

A 108 cubic inches
B 54 cubic inches
C 27 cubic inches
D 9 cubic inches

38 A right cone is placed on its circular base.


Which statement about the cone is incorrect?
F The view from the front is a triangle.
G The view from the bottom is a circle.
H The view from the top is a circle.
J The view from the left is a rhombus.

39 A cone has a slant height of $\mathbf{1 0}$ centimeters and a lateral area of $\mathbf{6 0} \pi$ square centimeters. What is the volume of a sphere with a radius equal to that of the cone?

A $102 \pi \mathrm{~cm}^{3}$
B $144 \pi \mathrm{~cm}^{3}$
C $288 \pi \mathrm{~cm}^{3}$
D $1,333 \pi \mathrm{~cm}^{3}$

40 Which line of reflection maps point $K$ at $(-2,2)$ to point $K^{\prime}$ at $(2,-2)$ ?
F $y=2$
G $y=x$
H $x$-axis
J $y$-axis

41 If the coordinates of $A$ are (1, 1) and the midpoint of $\overline{A B}$ is $(-2,0)$, then the coordinates of $B$ are -

A $(-0.5,0.5)$
B $(0.5,0.5)$
C $(-1,0)$
D $(-5,-1)$

42 Which transformation could move the triangle $P$ to triangle $P^{\prime}$ in a single step?


F Reflection over $x=4$
G Rotation about $(2,3)$
H Reflection over $y=4$
J Translation

43 Figure STARFIND is symmetric with respect to the $x$-axis. The coordinates of point $A$ are $(8,6)$. What are the coordinates of point $N$ ?


A $(8,-6)$
B $(6,-8)$
C $(-6,8)$
D $(-8,6)$

44 Parallelogram RSTV has coordinates $R(0,0), S(2,4), T(6,0)$, and $V(4,-4)$. Which ordered pair represents the intersection of the diagonals of this parallelogram? (The coordinate grid may be used to help answer this question.)


F $(2,0)$
G $(3,0)$
H $(3,1)$
J $(4,-1)$

## 45 A regular quadrilateral has what type of symmetry?

A Line symmetry only
B Point symmetry only
C Both point and line symmetry
D Neither point nor line symmetry

Answer Key-EOC021-M0110

| Test Sequence Number | Correct Answer | Reporting Category | Reporting Category Description |
| :---: | :---: | :---: | :---: |
| 1 | D | 001 | Lines and Angles |
| 2 | F | 001 | Lines and Angles |
| 3 | D | 001 | Lines and Angles |
| 4 | H | 001 | Lines and Angles |
| 5 | C | 001 | Lines and Angles |
| 6 | G | 001 | Lines and Angles |
| 7 | B | 001 | Lines and Angles |
| 8 | F | 001 | Lines and Angles |
| 9 | B | 001 | Lines and Angles |
| 10 | J | 001 | Lines and Angles |
| 11 | D | 001 | Lines and Angles |
| 12 | G | 002 | Triangles and Logic |
| 13 | A | 002 | Triangles and Logic |
| 14 | G | 002 | Triangles and Logic |
| 15 | C | 002 | Triangles and Logic |
| 16 | H | 002 | Triangles and Logic |
| 17 | D | 002 | Triangles and Logic |
| 18 | F | 002 | Triangles and Logic |
| 19 | C | 002 | Triangles and Logic |
| 20 | J | 002 | Triangles and Logic |
| 21 | B | 002 | Triangles and Logic |
| 22 | G | 002 | Triangles and Logic |
| 23 | A | 002 | Triangles and Logic |
| 24 | F | 003 | Polygons and Circles |
| 25 | A | 003 | Polygons and Circles |
| 26 | H | 003 | Polygons and Circles |
| 27 | D | 003 | Polygons and Circles |
| 28 | F | 003 | Polygons and Circles |
| 29 | C | 003 | Polygons and Circles |
| 30 | J | 003 | Polygons and Circles |
| 31 | B | 003 | Polygons and Circles |
| 32 | F | 003 | Polygons and Circles |
| 33 | A | 003 | Polygons and Circles |
| 34 | J | 004 | Three-Dimensional Figures |
| 35 | B | 004 | Three-Dimensional Figures |
| 36 | F | 004 | Three-Dimensional Figures |
| 37 | C | 004 | Three-Dimensional Figures |
| 38 | J | 004 | Three-Dimensional Figures |
| 39 | C | 004 | Three-Dimensional Figures |
| 40 | G | 005 | Coordinate Relations and Transformations |
| 41 | D | 005 | Coordinate Relations and Transformations |
| 42 | J | 005 | Coordinate Relations and Transformations |
| 43 | A | 005 | Coordinate Relations and Transformations |
| 44 | G | 005 | Coordinate Relations and Transformations |
| 45 | C | 005 | Coordinate Relations and Transformations |

Geometry, Core 1

| If you get this many items correct: | Then your converted scale score is: |
| :---: | :---: |
| 0 | 000 |
| 1 | 177 |
| 2 | 213 |
| 3 | 234 |
| 4 | 250 |
| 5 | 263 |
| 6 | 274 |
| 7 | 284 |
| 8 | 292 |
| 9 | 300 |
| 10 | 307 |
| 11 | 314 |
| 12 | 320 |
| 13 | 326 |
| 14 | 332 |
| 15 | 338 |
| 16 | 343 |
| 17 | 348 |
| 18 | 353 |
| 19 | 358 |
| 20 | 363 |
| 21 | 368 |
| 22 | 373 |
| 23 | 378 |
| 24 | 383 |
| 25 | 388 |
| 26 | 392 |
| 27 | 397 |
| 28 | 402 |
| 29 | 408 |
| 30 | 413 |
| 31 | 418 |
| 32 | 424 |
| 33 | 430 |
| 34 | 436 |
| 35 | 442 |
| 36 | 449 |
| 37 | 457 |
| 38 | 465 |
| 39 | 474 |
| 40 | 485 |
| 41 | 497 |
| 42 | 513 |
| 43 | 534 |
| 44 | 569 |
| 45 | 600 |

A total raw score (left column) is converted to a total scaled score (right column). The total scaled score may range from 0 to 600.

A scaled score of 400 or more means the student passed the SOL test, while a scaled score of 399 or less means the student did not pass the test. A scaled score of 500 or more indicates the student passed the SOL test at an advanced level.

